



Remark\\Twelve mark for every question and six mark for every branch.

Q1\ A\ Define and give example with it is solution for the following terms:

1-Semi-group 2- Great common divisor 3- Prime number

B\ Let $(P(x), *, \#)$ is a mathematical system which defined by:

(1) $A \# B = A \cap B$ (2) $A * B = A \cup B$ for all $A, B \in P(x)$. Does $(P(x), *, \#)$ is number system?

Q2\ A\ Prove that the mathematical system $(Z, +)$ is a belain group s.t $a + b = [m + p, n + q]$
For all $a, b \in Z$ and $a = [m, n]$ and $b = [p, q]$.

B\ Let $f(n) = a^n - 1$, $n > 1$. Then $f(n)$ is prime only if $a = 2$ and n is prime.

Q3\ A\ Prove that the mathematical system (Q, \leq) is totally ordered set.

B\ If $(x, a) = 1$ and $(x, b) = 1$ then $(x, ab) = 1$.

Q4\ A\ Prove that the mathematical system $(Q, +, \cdot)$ is a field of rational number.

B\ Let z, w are two complex number. Then $|z + w| \leq |z| + |w|$.

Q5\ A\ Cube of any integer is of the form $9K, 9K \mp 1, 9K + 8$.

B\ Two integers a and b , both not zero are relatively prime iff $1 = ax + by$ for some $x, y \in Z$.

Rest of luck