Ministry of Higher Education & Scientific Research Muthanna University College of Science Department of Mathematic & Com. application



Subject: Foundation mathematics II Stage: first Date: / /2017 Time :

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'((Assessment of the final exam for the second semester))^{0.06.2017} Academic year 2016 -2017

<u>Remark</u>\\Twelve mark for every question and six mark for every branch. Q1\ A\Define and give example with it is solution for the following terms: 1-Semi-group 2- Great common divisor 3- Prime number

B\Let (P(x),*,#) is a mathematical system which defined by: (1) $A#B = A \cap B$ (2) $A*B = A \cup B$ for all $A, B \in P(x)$. Does (P(x),*,#) is number system?

Q2\ A\ Prove that the mathematical system (Z,+) is a belain group s.t a+b = [m+p, n+q]For all $a, b \in Z$ and a = [m, n] and b = [p,q]. B\ Let $f(n) = a^n - 1$, n > 1. Then f(n) is prime only if a = 2 and n is prime.

Q3\ A\ Prove that the mathematical system (Q, \leq) is totally ordered set.

B\ If (x,a) = 1 and (x,b) = 1 then (x,ab) = 1.

Q4\ A\Prove that the mathematical system (Q,+,.) is a field of rational number. B\ Let z, w are two complex number. Then $|z+w| \le |z|+|w|$.

Q5\A\Cube of any integer is of the form $9K, 9K \neq 1, 9K + 8$.

B\Two integers a and b, both not zero are relatively prime iff 1 = ax + by for some $x, y \in Z$.

Rost of luck